# **Investment Product Research**

# A DESCRIPTION OF CALCULATIONS

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INTRODUCTION

Investment Product Research offers clear and fair quantitative research on structured products. Our primary aim is to give advisers and investors an indication of the risk and return that a product offers, relative to other products.

Our analysis can therefore be used to RANK products, but does NOT provide reliable information on FUTURE returns or probabilities of events.

Our analysis allows products to be filtered to identify a short list of products that may be suitable, and then ranked using a number of different measures to help identify the product that best meets the investor's requirements.



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# 1. Methodology

We measure risk and return using historical data only:

- We use publicly available data that is available through external sources such as Bloomberg
- Our analysis is fully transparent, objective and verifiable
- There is no need for specialist derivatives knowledge
- We are not required to make any assumptions, estimates or judgments

#### We use straightforward methodologies, applied consistently across all products

- We offer clear analysis of the risks and returns a product offers
  - We calculate the product's "volatility"
  - We map this volatility to a number of risk scores
  - We calculate a range of "expected" returns that a product offers
- Our analysis makes product comparison straightforward;
  - compare products to benchmark equity / bond portfolios
  - compare products from different issuers
  - compare products with exposure to different underlying markets
- There is no need for specialist statistical or mathematical knowledge to understand the analysis
- Our analysis metrics are consistent with the risk information offered by funds in their Key Investor Information Documents (KIIDs)
- Our analysis metrics are consistent with mainstream financial planning tools and processes

# 2. Product Analysis

Product analysis is all interactively available online and can be accessed digitally using our APIs, or pdf document generator. The analysis is updated weekly throughout product life, reflecting the current product price and the latest levels of the underlying assets and other market data – please refer to the "Dealing with products post-strike" section for further details.

#### **MULTIPLE SCENARIOS**

We test products under different scenarios

- Historic Back-test; an analysis of the risks and returns offered by a product that uses the actual past performance of the underlying assets
- Future Stress-test; the same analysis but on multiple re-sampled paths of the historical returns of the underlying data
- Credit Adjusted Future Stress-test; an adjusted Future Stress-test where the risks and returns are adjusted to reflect the possibility of the issuer defaulting
- UKSPA analyses (Bear, Neutral and Bull); we do not discuss this further as details can be found on the UKSPA site
- PRIIPs; details are given in a later section

#### I. Historic Back-test methodology

We use daily closing levels of a product's underlying(s) as far back as possible to analyse the returns that a product would have offered had it been available in the past.

To illustrate, we describe how on 15<sup>th</sup> May 2015 we would have back-tested a 6 year autocall with annual kickouts from Year 2 and a 50% American soft protection barrier, with an underlying whose first data point is 31<sup>st</sup> December 1986:

- the first 6-year cycle we look at is therefore 31<sup>st</sup> December 1986 to 31<sup>st</sup> December 1992
- the second is 2nd January 1987 to 2nd January 1993 and so on, each cycle starting and ending on a trading day
- the last cycle is 15<sup>th</sup> May 2009 to 15<sup>th</sup> May 2015 as this is the last complete 6 year term
- There are 5770 such cycles

For each cycle, we first check if the product would have kicked out in Year 2. If so, it is recorded as a Year 2 early maturity and no further analysis is needed for that cycle. If not, we then check if it would have kicked out in Year 3 and so on through to Year 6.

We cannot select cycles starting later than 15<sup>th</sup> May 2009 as the six year term would not have been completed. This is the case even when we know that on some of those occasions the product would have matured early. To include such cycles would be to "cherry pick" as only those that had matured early would be included; cycles where the product would not yet have matured and which could end in a capital loss would be left out and therefore would present a misleading result.

We can then analyse the outcomes and record how many of the 5770 cycles would have resulted in a Year 2 kick out, Year 3 kick out, Year 4 kick out, Year 5 kick out, Year 6 growth payment, a maturity payment equal to the capital invested or a capital loss at maturity.

The results can be presented as a percentage of the population of 5770 cycles. For example, 4720 Year 2 kick outs is 81.8% of the 5770 possible start dates; similarly 58 occasions where a capital loss occurred is 1% of the possible start dates.

The same principles can be applied to other structures. For example, with the same basic product shape linked to the several indices, we would start from the earliest common data date for all indices. Although the time span is the same, there will be fewer observations, as the back-test can only use a start date when both indices are quoted.

Our research is not restricted to fixed start dates however. It will facilitate a time period of the user's choosing. For example, if an analyst were to assume that only the last 10 years of data were relevant, on our site they could set the start date to reflect only this period of data. The number of cycles would then be reduced to only the last 10 years.

#### II. Future Stress-Test

Having only 1 sample of history constrains risk analysis:

- For example, some products would have had no, or a very small number of cycles that would have led to capital losses, despite the fact that the product structure has clear downside exposure and the fact that the investor is able to earn a significant additional potential return from assuming this risk.
   Placing such products in a low risk category may seem inappropriate
- Other products might have a structure that captures a current pricing opportunity to meet investor needs but which back-testing might show as having a poor historical record. Placing such products in a high risk category may seem equally inappropriate

Put another way; past performance is not a reliable indicator of future performance and should not be used to assess future returns or risks. Nobel prize-winner Paul Samuelson (and many other leading economists) highlighted the fallacy in simply taking realised market returns (as the Historic Back-test does) as statistically significant proof of performance – statistically speaking, history is just one sample from a much larger distribution of possibilities.

Resampling the available data is a well-established<sup>1</sup> way of representing the true underlying distribution of possibilities, enabling a statistically more correct assessment of risk. Resampling is a process that is simple, straightforward and robust.

As outlined in the Historic Back-test section above, there are 5770 dates on which a six year product might have started and reached the end of a six year term. This is just one dataset. Resampling allows for the creation of multiple datasets which explore more fully the range of possible movements in the underlyings.

In order to determine the possible future movement in the underlying, we look at what the range of daily movements has been in the past for the index and use these to create new index series. On most days the Index does not move by large amounts – it may go up a little, go down a little or remain flat. On other days, the daily change might be more exaggerated and on comparatively fewer days there will be extreme movements.

The first step is to compile a new dataset from the information that we have. We can set the new initial index price base level at 100.

A particular date is selected at random from all of the possible start dates in the data history that we are using<sup>2</sup>, for example date 3214. The close of business level on date 3214 is recorded and compared to the level at close of business on day 3215. This gives us the movement for the Index on that day. Let's say that it was 1% up.

The Index level at the end of the first "day" of our new index is therefore 101 (i.e.100 increased by 1% or 100 x 1.01). This is repeated until we have enough simulated data for the product's remaining time to maturity.

As the selection is random, any one day return can be selected again, and so could be used more than once as part of the resampling process. Some daily returns may not get selected at all. We then carry out back-testing on the newly constructed dataset in exactly the same way as we did for the single historical back-test of the actual index performance.

We repeat this process multiple times until the results we get are stable<sup>3</sup>, typically in the region of 100,000 iterations. At this point we can be confident that the values that we are able to derive from the resampling process will represent the likely future range of returns of the underlying assets, that this range will remain

<sup>&</sup>lt;sup>1</sup> For example, resampling relies on the well-proven (weak) efficient markets hypothesis, as do the entire fund management and derivatives industries

<sup>&</sup>lt;sup>2</sup> 1992–12–31 is our standard start date for the data window we resample from

<sup>&</sup>lt;sup>3</sup> i.e. further iterations would not bring about statistically meaningful changes in the results

constant, and so the results that we derive from the stress-test will not vary materially from one test to another.

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This resampling process means the much larger number of potential histories tested gives a more detailed view of the distribution of potential product outcomes and therefore enables more robust estimates of performance statistics.

#### III. Credit Adjusted Future Stress-Test

We also calculate a set of risk and return numbers that reflect any additional risk that an investor is exposed to from possible issuer default.

For each single cycle we assume that the final value is either

- The value that we have calculated using the re-sampled data
- 40% of the value calculated using the re-sampled data

The process is random, but the proportion of cycle results that are adjusted down will be based on the chance of default that we calculate. This process that we use implies that the issuer is as likely to default if the underlying assets have increased in value as when the underlying assets have fallen in value.

The chance of default is calculated using the issuer's CDS levels, and an assumed 40% recovery rate. The 40% recovery rate assumes that in the event of issuer default investors will receive 40% of the value of the product when it matures. 40% is a market standard recovery rate that is typically used to calculate these figures; expected returns are not very sensitive to the choice of assumed recovery rate.

The credit adjustment will reduce the expected gains and reduce the chance of a gain since if there is a default, some of the instances where an investor would have made a profit will now be loss making. The credit adjustment will both increase the chance of a loss, and increase the expected loss. As a result the credit adjusted risk-return ratio and Win Lose ratios will both be lower.

# DEALING WITH PRODUCTS POST-STRIKE

The analysis described above is applied equally to post strike products. It is useful nevertheless to describe how products present themselves to the analysis once they have struck. Basically, post-strike, a product now has fixed strikes, with a time to maturity that gradually decreases. For example a product with a kickout barrier on the first anniversary of 100% will have a barrier of 900.00 if this is the closing price on the strike date. If we evaluate this product 9 months later, when the underlying has a closing price of 1000.00:

- This barrier level is now 90% of the prevailing spot level
- So in our simulations we set this barrier level to 90% of the simulated starting level of the underlying
- And we set the barrier observation date to be 3m in the future, since 9m have already elapsed

In this way we analyse a product as it really is on the evaluation date. Similar calculations are used to reflect product features that are part-way through, for example, an averaging period, or a lookback period etc.

#### **USER-SPECIFIED PARAMETERS**

Rather than use historical or resampled data, users can elect to use, for any particular product, their own parameters. Currently we provide a standard diffusion process (multivariate geometric Brownian motion "GBM") and users can enter their own drift rate curves, volatility surfaces and correlation matrices. All of these are accessible from our Admin page.

As a result, each user has their own private set of global parameters: in other words there is, for example, one SX5E volatility surface which will apply to all that user's user-specified-parameters products.

Since user-specified parameters make market-wide product comparison difficult, any product using user parameters will not be visible on the IPR public Listing; it will still of course be visible on the Listing for that logged-in user.

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# 3. Output

#### **PRODUCT LIST**

The Product listing gives searchable and sortable details of the entire product database: users can screen and filter products, change column headings, and:

- choose which analyses to display (eg PRIIPs, UKSPA)
- choose which analysis metrics to use as sortable column headings
- view detailed analysis of risk and return
- view detailed probability of early maturity and barrier breach
- generate full PDF reports

#### SCREENING PRODUCTS

Each investor will have different requirements, their attitude to risk will be different and they will have a different capacity for loss. The variables that we publish will allow unsuitable products to be eliminated from consideration.

For many investors product risk is one of the most important suitability factors. We calculate a number of ways to look at risk: volatility (and its mapping to a range of risk scores), estimated "worst case" returns and payoffs, the chance of loss, and so on.

Investors are of course concerned about the returns that they should expect; they may want to eliminate products that do not offer enough potential return.

Both the risk and return scores can be used with, and without, a credit adjustment. Our credit adjustment process uses the issuer's bond spreads and market CDS rates. These may be rates the investor agrees with, or which they feel does not reflect the creditworthiness of the issuer. We also give issuer credit rating, which is another possible screen.

#### **RANKING PRODUCTS**

Having identified if a product meets an investor's minimum requirements there are a number of ways they can be ranked: we offer a comprehensive set of risk/return metrics as sortable analysis columns; for example, investors can rank products on the overall expected return, or on the positive return that they may receive; other investors could alternatively rank products based on a chosen risk score or volatility.

Our online analysis has these sections

- Efficient Frontier
  - All screened products are plotted on a scatter chart whose axes can be chosen by the user; we also plot a guide line between a cash asset and an equity index
- Product-by-product Tables
  - Product terms and issuer details

- Summary Statistics
- Payoff analyses
- Charts
  - Historic backtest charts
  - Future stress-test chart
  - Performance chart, where historic product prices are available

# 4. Product Listing entry

Each product has a row in the Listing, which can be clicked to give details:

#### Static data

Issuer	Credit Suisse AG					
IssuerRating	A					
Initial Valuation Date	2013-06-21					
FinalDate	2019-06-21					
GeneralDescription	Growth return					
	40% at maturity if Final Index					
	Level at least 75% of Opening					
	Level					
	Capital protection					
	60% European					
Bid (Source:Bloomberg)	131.59 2017-09-22					
Ask (Source:Bloomberg)	132.59 2017-09-22					
Fair Value	136.48 2017-09-22					
Analysis Reference Price	132.59					
▼ more reference data						

<ul> <li>more reference data</li> </ul>	
Shape	Digital
Objective	Enhanced Return
CapitalAtRisk	yes
Maximum Term	6 years
TaxTreatment	CGT
PrimaryOfferStart	2013-06-19
PrimaryOfferEnd	2013-06-19
Currency	GBP
Settlement	Crest
Listing	London
Isin	X50927210608
Public Offer	yes
Retail or Professional	yes
Secondary	yes
UseUserParams	no
Asset Type	Security
Collateralised	no
CreditEnhanced	no
DepositGteed	no
Delta Down	0.12
Benchmark	TUKXG
Vega	-0.17

I N V E S T M E N T P R O D U C T R E S E A R C H

# Summary metrics

The columns of these tables can be chosen by the user:

P R O D U C T R E S E A R C H

Date start		1992-	12-31 1	985-12-31
Date end		2017-	09-22 2	017-09-22
	Str	esstests		Historic Backtest
		IPR Market		
	IPR Market	and	PRIIPs Market	Market
	Risk	Risk	Risk	Risk
		Returnin	netrics	
Expected Return (%pa)	2.9	2.5		2.9
Arithmetic Return (%pa)	2.9	2.7		2.9
Coupon Return (%pa)	0.0	0.0		0.0
		• n	nore Retu	irn metrics
		Risk me	etrics	
Volatility of Returns	1.7	3.8	NC	1.9
Average Worst 5% Payoff	129.1	116.9	NC	127.6
		•	more R	isk metrics
	ber	ichmark-r	elative R	isk metrics
		Time m	etrics	
Expected Term to Maturity	1.7	1.7		1.7
		•	more Ti	me metrics

# Scenario metrics

	Stresstests						His	toric Back	test	UK100				
		IPF	R Market Ris	k	IPR Mar	ket and Iss	uer Risk	PRII	Ps Market	Risk		Market Ris	k	6116.17
Desc	Levels	Prob	PayoffAr	nReturn	Prob	Payoff.4	AnnReturn	Prob	Payoff.	AnnReturn	Prob	Payoff/	AnnReturn	
Maturity - above 75%	75.0E	98.7	140.0	3.2	98.7	139.4	2.9	99.4	140.0	3.6	98.4	140.0	3.2	62.7%
Maturity - 60% barrier hit	60.0E	0.1	56.5	-38.7	0.1	56.1	-39.0	0.0	56.6	-30.1	0.0	0.0	0.0	50.2%
Maturity - below 75%, above 60%	100	1.2	100.0	-14.9	1.2	99.6	-15.1	0.6	100.0	-10.5	1.6	100.0	-14.9	83.7%

These tables are updated after the strike date to show barrier levels, trigger levels and other reference data as specific levels and also as a % of the current underlying level(s).

# Coupon metrics

			Future Str	esstest		Historic B	acktest
Desc	Level	Prob	CondProb	Payoff	ProbO	ondProb	Payoft
Income 2017-11-10	80.0E	97.6	97.6	1.5	97.2	97.2	1.5
Income 2018-02-13	80.0E	89.4	89.4	1.5	89.8	89.8	1.5
Income 2018-05-10	80.0E	84.6	84.6	1.5	85.9	85.9	1.5
Income 2018-08-10	80.0E	81.3	81.3	1.5	83.1	83.1	1.5
Income 2018-11-12	80.0E	78.8	78.8	1.5	79.4	79.4	1.5
Income 2010-02-12	00 0E	76.0	76.0	1.5	70 2	70 0	1.5

<ul> <li>CouponHistogram</li> </ul>					
Coupon Histogram					
Str	resstestB	acktest			
NumCoupons	Prob	Prob			
0	0.3	0			
1	1.5	1.1			
2	1.8	1.6			
3	1.9	1.4			
4	1.9	1.6			
-					

# 5. Calculations

Our Expected Return reflects the geometric average of the returns realised in repeated simulations of investment in the product. We use the geometric average because it produces a CAGR figure, which can be compared across products and asset classes with different time horizons. Note that all our other return numbers, such as conditional gain, are arithmetic averages (of the returns realised in repeated simulations of investment in the product) and therefore should not be interpreted as CAGR figures.

# **Return calculations**

#### Expected Return (%pa)

The expected return is the annualised expected return obtained from all simulated product episodes. For example, an expected return of 41.85% after 6 years is the equivalent of 6% per annum ( $1.06^{6} - 1 = 41.85^{\circ}$ ). But for kick-outs, the payoff P can occur at different times T and with an associated probability. The return is therefore calculated as an annualised return

# $\exp(\sum_{i=1}^{N} ln(P_i) / \sum_{i=1}^{N} T_i) - 1$

Where  $P_i$  is the payoff<sup>4</sup> at time  $T_i$  of the i-th product instance

The expected return reflects all of the outcomes, good and bad, that the product has delivered under each scenario. As such it is a good reflection of the return that the product will offer.

#### Arithmetic Return (%pa)

The arithmetic return is the annualised return based on the expected payoff and duration:

# $(\Sigma p_j P_j) \wedge (1 / \Sigma p_j T_j) - 1$

Where p<sub>j</sub> is the probability of scenario j which occurs at time T<sub>j</sub> and whose arithmetic average payoff is P<sub>j</sub>

It reflects the average payoff, annualized by the average time to maturity, and is typically somewhat higher than the Expected Return above.

#### CouponReturn

This is the arithmetic average of the simulated annualized returns, where each such return references ONLY the sum of (a) the value of all product coupons (forward-valued to the payout date if necessary) and (b) a FULL repayment of the product notional – so the coupon return will include any "pull-to-par" return.

#### IRR

All simulation cashflows are accumulated and the IRR is their annualized internal rate of return; ie the return which gives a zero present value of all cashflows.

#### Excess return (%pa)

<sup>4</sup> eg 1.15 representing a 15% gain

Arithmetic return minus a "benchmark" return of:

(6y GBP swaps) + 5yCDS/2 + (Product volatility/TUKXG volatility)/(TUKXG ArithmeticReturn - 6y GBP swaps) The "benchmark" return reflects a fair hurdle for product volatility and issuer funding/credit.

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# Expected Payoff

# $\Sigma p_t P_t$

For example, suppose a product pays:

- 40% growth at maturity if the Index is at or above its Initial Level,
- Capital return only if Index is below its Opening level but no breach of the protection barrier, and
- Capital reduced if the protection barrier is breached

Let's say our results show 75% of occasions resulted in a 40% payment, 20% resulted in capital return only (0% growth) and 5% ended in a loss averaging 43%, the expected pay off would be 75%\*40% + 20%\*0%+5%\*-43% = 27.85%.

The same calculations can be used for kick out plans but using the individual autocall coupons payable in any one year multiplied by the proportional incidence of autocalls in that year

#### Win Lose Ratio

This is the ratio of the total annualised returns of (1) all product instances with positive returns; (2) all product instances with negative returns<sup>5.</sup> It measures the relative amounts of "win" and "lose" returns.

# $\Sigma R_{gain} / \Sigma R_{loss}$

Where:

Rgain is the return for a product instance that was a gain

Rloss is the return for a product instance that was a loss

The Win/Lose ratio is a ratio that we have developed to help rank products. A high Win Lose ratio means that the product offers a greater number of wins for each unit of loss. It is an alternative to the risk / return ratio and reflects the probability, term and scale of winning and losing outcomes. We developed this ratio to better reflect the variable term that is a common feature of structured products, but it can just as easily be used to evaluate equities, bonds and other assets.

Features of WinLose:

- Easy to understand and interpret
- Easy to estimate
- Combines all "moments" of the returns distribution: mean,variance,skew,kurtosis and so on; this contrasts with some statistical measures (eg modified VaR) which use unstable<sup>6</sup> statistics (ie summaries) of the data; WinLose uses all the data and therefore provides a more comprehensive product ranking than SharpeRatios, VaR,modifiedVaR, etc

<sup>&</sup>lt;sup>5</sup> An alternative description is the ratio: ExpectedConditionalGain/ExpectedConditionalLoss

<sup>&</sup>lt;sup>6</sup> use cubes and fourth powers of the data

• Produces sensible product Ranking: a product with a higher WinLose is better<sup>7</sup>

### Risk Return Ratio

This is the ratio of expected return to volatility, and shows the expected return for every unit of risk.

The risk return ratio uses our volatility calculation as the measure of risk, and the expected return calculation as the measure of return.

#### Combo Ratio

This is the ratio of non-credit-adjusted expected return to credit-adjusted volatility, and shows the expected return for every unit of risk *including credit risk*.

The risk return ratio uses our credit-adjusted volatility calculation as the measure of risk, and the expected return calculation as the measure of return.

#### Conditional Gain (%pa)

# $\Sigma R_{gain} / N_{gain}$

For outcomes that result in a gain (defined as an annualized return >= 0), this shows the average size of that gain.

Where:

Ngain is the number of product instances that resulted in a gain

Rgain is the annualised return for a product instance that was a gain

The conditional gain is the average gain for instances where there has been a gain. It is a measure of the potential profit of a product.

## Probability of Gain

Ngain / N

Where:

Ngain is the number of product instances that resulted in a gain (where the payoff is equal to or exceeds the initial investment) compared to the total number of product cycles.

The probability of gain is self-explanatory. It is a calculation of the proportion of the outcomes that have resulted in a return equal to or greater than the current asset prices. For new products offered at 100%, this will mean that this is the proportion of outcomes where the final value is equal to or greater than 100%. Once a product has struck this will reflect the proportion of outcomes where the final value is greater than the current product price.

<sup>&</sup>lt;sup>7</sup> The only assumption is that more is better; there are no risk-preference or utility assumptions



### Expected Gain

 $(N_{gain} / N) \times (\Sigma R_{gain} / N_{gain})$ 

Which is equivalent to the Probability of Gain multiplied by the Conditional Gain, annualised.

Multiplying the conditional gain by the probability of a gain generates an expected gain, or a probability adjusted gain. This reflects both the chance of a gain, and the scale of the gain that is expected.

#### Expected Gain Payoff

Same as ExpectedPayoff, but only for those  $P_t \ge$  initial investment.

#### Conditional Strict Gain (%pa)

Same as ConditionalGain, but only for those R<sub>gain</sub> > 0 (ie strictly greater than zero).

#### Probability of Strict Gain

Same as ProbabilityOfGain, but only for those product instances whose payoff is strictly greater than the initial investment.

#### Expected Strict Gain Payoff

Same as ExpectedPayoff, but only for those  $P_t >$  initial investment.

#### Probability of No Gain or Loss

 $(N_{zero} / N)$ 

Where N<sub>zero</sub> is the number of product instances whose payoff is exactly equal to the initial investment.

# **Risk calculations**

#### Volatility of Returns

Since risk should measure downside, we believe volatility should be measured from the left tail of a product's distribution. We use a version of the CESR methodology that was proposed to calculate the volatility of a structured product so that they can be ranked using the same volatility based Synthetic Risk and Return Indicator (SRRI) as funds. We find a normal distribution with the same arithmetic average return whose left tail (or Expected Tail Return) matches that of the product's distribution of returns:

- Start with the distribution of annualized returns from the product simulations described above;
   please note that the following calculations use arithmetic averages
- Compute the arithmetic average annualised return for all product instances below the 90th confidence level (the left tail) – call this the product's Expected Tail Return (see definition above)



 Find the standard deviation of a normal distribution of returns (with mean the Expected Return) whose Expected Tail Return below the 90% confidence level is the same as the product's Expected Tail Return; this quantity is the volatility

Suppose a product has an arithmetic average return of 5%<sup>8</sup>, ExpectedTailReturn of minus 8%, and duration of 4y. A normal distribution with mean 5% must have a standard deviation 7.4% to produce an ExpectedTailReturn of minus 8%<sup>9</sup>. Hence the product's annualised returns have a volatility of 7.4%. The product's payoff volatility is therefore 14.8% since the volatility scales with root time ( $\sqrt{4}=2$  in this case). A more detailed example is given as Appendix A.

Calculating volatility this way lets us compare the riskiness of a product's potentially unusual payoff profile (non-normally distributed) with the riskiness of a fund or other asset with a more normal distribution.

It is important to note that the volatility calculation is not an estimate of the fluctuation of day-to-day returns but instead a reflection of the risk of a product. The calculated volatility for equity based products will reflect the propensity for equity markets to occasionally fall significantly. These so called "fat tails" will increase the calculated volatility of equity based products

The calculated volatility can and will vary once the product has struck, and the terms have been fixed.

#### **Risk Scores**

For our standard risk score we have used the risk buckets that are prescribed by CESR. These buckets define a 1 to 7 risk score based on volatility. We also provide a score based on a linear scale from 1 to 10. We use the volatility that we have calculated using the process above. The table below describes the upper and lower volatility bands for each bucket.

<sup>&</sup>lt;sup>8</sup> This is not our ExpectedReturn which is a geometric CAGR-type number as described; typically you can obtain the arithmetic average return as the probability-weighted average return from our scenarios tables

 $<sup>^{\</sup>rm 9}$  ExpectedTailReturn for the left p% tail of a standard normal distribution is, in Excel terms,

<sup>=</sup>NORM.S.DIST(NORMSINV(p),FALSE)/p or minus 1.75 for p=0.1; we can in this case equate to the normalized shortfall of (5 minus -8)/volatility, ExpectedTailReturn so that volatility = 13/1.75 = 7.4

VOLATILITY	RISK SCORE	
0%	0.5%	1
0.5%	2%	2
2%	5%	3
5%	10%	4
10%	15%	5
15%	25%	6
25%		7

VOLATILI	RISK SCORE 1to10	
0%	2.6%	1
2.6%	5.2%	2
5.2%	7.8%	3
7.8%	10.4%	4
10.4%	13.0%	5
13.0%	15.6%	6
15.6%	18.2%	7
18.2%	20.8%	8
20.8%	23.4%	9
23.4%	26.0%	10
26.0%		11

Where product volatility falls within a range, we interpolate the Risk Score linearly so that 18% volatility, for example, translates to a Risk Score of 6.3.

The risk score for a structured product allows advisers to calibrate the risk of a structured product versus the risk of a fund. Although the method of calculation is different (the volatility of funds is calculated using historic daily returns) the risk score has been designed to be comparable.

#### VaRxxReturn

The (100-xx)<sup>th</sup> percentile annualized return from all product episodes; for example the VaR90Return is the 10<sup>th</sup> percentile annualized return, for example, the 100<sup>th</sup>-worst annualized return from 1000 episodes.

#### Expected Tail Return10 (%pa)

$$\sum_{i=1}^{N*0.1} R_i / (N*0.1)$$

This is the average of the worst 10% annualised returns R. So if there are 100,000 instances we sort them and calculate the average of the 10,000<sup>th</sup> lowest returns. This downside measure risk measure suits investors with a "capacity for loss" approach.

While VaR is commonly used to estimate worst case results<sup>10</sup> we prefer ExpectedTailReturn because it is a more stable, reliable and representative indication of the worst case that an investor will suffer. The discontinuous nature of the distribution of final values for a structured product means that the VAR figure can jump significantly in response to very small changes in the product terms whereas ExpectedTailReturn will not.

#### Conditional Loss (%pa)

 $\Sigma R_{loss} / N_{loss}$ 

<sup>&</sup>lt;sup>10</sup> for example, many capacity-for-loss risk scales; also the Committee of European Securities Regulators (CESR) proposed VaR to calculate the equivalent volatility of a product



For outcomes that result in a loss, this shows the average size of that loss.

Where: Nloss is the number of product instances that resulted in a loss

The conditional loss is the loss that can be expected from the instances where there is a loss. It is useful as a measure of the scale of the loss that can be expected if there is a loss.

### Probability of Loss

## N<sub>loss</sub> / N

Where: Nloss is the number of product instances that resulted in a loss compared to the total number of product cycles.

The probability of loss is self-explanatory. It is measure of the proportion of instances in which the product has generated a loss.

#### Expected Loss (%pa)

# (Nloss / N)×( $\Sigma R_{loss}$ / Nloss)

Which is equivalent to the Probability of Loss multiplied by the Conditional Loss, annualised.

By multiplying the conditional loss with the probability of loss, the expected loss is a reflection of the risk an investor faces.

#### Average payoff when there is a loss

The arithmetic average of payoffs from all product episodes where the investor receives less than they paid.

#### **Benchmark-relative calculations**

Each product can choose its benchmark to be either a flat hurdle rate, like 2.5%pa, or a market underlying (eg SP500 index). As it records a product "episode" return, our analysis also records the corresponding benchmark return, so that we can calculate for each episode:

- "RelativeReturn" product return minus benchmark return
- "RelativeAnnualisedReturn" product annualised return minus benchmark annualised return
- "RelativeLogReturn" product log return minus benchmark log return; for example if the product episode pays 150 after 5 years on a 100 notional, and the benchmark is a 2.5% hurdle rate, the RelativeLogReturn will be ln(1.5) minus ln(1.025)\*5

#### BenchmarkProbShortfall

The proportion of product episodes with negative RelativeReturn

#### BenchmarkCondShortfall(pa)

The arithmetic average of the negative RelativeReturns, annualized using the product's Expected-term-tomaturity

## BenchmarkCondOutperf(pa)

The arithmetic average of the positive RelativeReturns, annualized using the product's Expected-term-tomaturity

#### BenchmarkRelativeCAGR(pa)

This represents the annualized difference in the rate of wealth creation between the product and the benchmark.

Briefly it is the CAGR of the RelativeLogReturns, similar to the IPR ExpectedReturn described earlier. More exactly, we sum all episodes' RelativeLogReturns and divide by the sum of the episodes' years to expiry; this is a continuous rate of return, which we then convert to an annual rate.

#### BenchmarkRelativeOutperfPV

We have 2 implementations (apologies for keeping PV in the name regardless – your platform provider can tell you which is being used):

- a) The arithmetic average of the positive product PVs, discounting at the benchmark annualised return. Here we PV each product episode's cashflows at the benchmark annualised return for that episode<sup>11</sup>
- b) BenchmarkProbOutperf \* BenchmarkCondOutperf

#### BenchmarkRelativeUnderperfPV

We have 2 implementations (apologies for keeping PV in the name regardless – your platform provider can tell you which is being used):

- a) The arithmetic average of the negative product PVs, discounting at the benchmark annualised return
- b) BenchmarkProbUnderperf \* BenchmarkCondUnderperf

#### BenchmarkRelativeAveragePV

We have 2 implementations (apologies for keeping PV in the name regardless – your platform provider can tell you which is being used):

- a) The arithmetic average of the product PVs, discounting at the benchmark annualised return, similar to the IPR ArithmeticReturn.
- b) The arithmetic average of the RelativeReturns, annualized using the product's Expected-term-tomaturity

# Time calculations Expected term to maturity

# $\Sigma p_t T_t$

For a kick-out contract, this calculates the expected maturity time, using the same principles above.

<sup>&</sup>lt;sup>11</sup> Like all discounting, another way to think of the result is the ratio of (a) product return at maturity (with income forward-valued); and (b) the benchmark return at that maturity (for example the forward bond value (1+hurdleRate)^years-to-maturity)

Many structured products have early call features. Advisers can take the expected maturity into consideration when evaluating the suitability of a product

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#### Probability of the earliest maturity

 $\Sigma N1 / N$ 

Where N1 is the number of product instances that matured at the earliest possible maturity date.

#### Probability of any early maturity

 $\Sigma N_t / N$ 

Where:

Nt is the number of product instances that matured early at time t

N is the total number of product instances

This calculates the probability of the product kicking out early on any one of the regular measurement dates.

# Fair value calculations

#### FairValue

Each week we calculate *approximate* fair values for each product with an ISIN and whose underlyings are in the set of underlyings (FTSE100, Eurostoxx50, SP500), as follows:

- Market data is COB the last trading day of the week for the UnderlyingsSet, and comes from a variety of sources, including Bloomberg
- Volatility surfaces are fit to market data using a modified "SVI" methodology, which fits parameterized curves to each time slice
- Correlations are implied from prices of traded structured products
- Funding spreads are guesstimated from CDS curves and from the nature of the product; typically we use 100% of the CDS spread to nominal maturity where a product has no early call features and will therefore run to full maturity; autocalls and other early call products typically use 50% of the CDS spread; we make no other adjustment for credit (ie we effectively do a FVA and not a CVA)
- Fair values are the average discounted (including funding spread) monte carlo payoffs

## **API and Excel calculations**

If you have access to our API or Excel sheets, there are some additional calculations:

#### Chance of issuer default in 1y (API)

Bloomberg's DRSK function calculates the probability that an issuer will default within the next year, using current levels of the issuer's gearing and share price volatility; it can therefore be calculated realtime, provided the issuer's equity is traded.

The issuer's equity share price behaviour, together with its outstanding debt, is used to model the behaviour of the firm's total assets (in more detail, the issuer's equity is viewed as a call option on the firm's total assets, with a strike price equal to its liabilities; this enables the implied total assets to be calculated). In this model, default occurs when total assets fall below liabilities at any time in the next year. Bloomberg applies a final transformation to these chance-of-defaults to ensure they reflect historical actual default rates of firms of similar credit rating.

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### Annualised return histogram (API,Excel)

We allocate each episode's annualized return to buckets 5% wide, with end buckets at -10% and +10%.

#### Headline return (API, Excel)

The annualized return represented by the difference between the first and second conditional payoffs, for a product with at least 2 conditional scenarios with fixed payoffs, for example autocalls.

# **Complexity calculations**

Investment advisers are required to ensure that products are suitable for each client. One element of this assessment is to match the complexity of a product against the financial sophistication of each client. The complexity score is a way of grading each product. Our complexity rating is a simple additive score. We have defined a value for each feature a product may have. The complexity score is a sum of the values. The table below describes the value we have given each feature.

Payout Score		Underlying Score		Protection Score	2	Asset Score	
Autocall (same triggers)	4	Single major index	1	100 pct	1	Note	1
Phoenix	5	Single other	3	SCARP European	3	WarrantLinked	3
Digital	2	Multiple	2	SCARP American	4	UCITS	3
Upside	1	Multiple complex	8	SCARP no barrier	2	SPV	5
Accrual	3				_		-
Reverse convertible	2					CreditLinked	6
Supertracker	1					Multiple Issuers	2
Synthetic zero	1					Collateralised	1
Rainbow	3						
Twin win	3						
Partly Paid Warrant	3						
Himalaya	3						
Different triggers	1						
Unconditional income	1						
Conditional income	3						
Averaging	2						
Lookback	5						



Inverse exposure	3		
Capped	1		
Multidirectional exposure	5		
Leveraged downside	2		

# **PRIIPs**

We follow the calculations set out in the current RTS <u>https://www.esma.europa.eu/sites/default/files/library/jc 2016 21 final draft rts priips kid report.pdf</u>

The results are shown in the "PRIIPs Market Risk" column in the main analysis table (click a product's row) – you may first need to select the PRIIPs analysis in your Profile page. We necessarily do 3 sets of bootstrap analysis:

- a) Volatility is calculated using riskfree drift rates for the underlyings
  - "Volatility" in this table column is the PRIIPs VaR-equivalent volatility ("VEV")
  - "RiskScorePriips" gives the MarketRiskMeasure corresponding to this VEV
- b) All other results (including those for the PriipsScenarios) use real world drift rates, bootstrapping returns from the historical data window (typically 5 years); in particular
  - "RiskScore" uses:
    - i. 5y historical data
    - ii. Real world drifts
    - iii. IPR's volatility calculation (Section 5)
    - iv. IPR's volatility buckets (Section 5)
  - "Var90Return" is the 10<sup>th</sup> percentile from the distribution of real world annualized returns
  - "Var50Return" is the 50<sup>th</sup> percentile
  - "Var10Return" is the 90<sup>th</sup> percentile
- c) PRIIPs Stresstest scenario, using the stresstest volatility and drift rates mandated by the RTS

## **Priips Summary**

We provide a summary of the required information for PRIIPs in 2 ways:

- a) Via an API, for example: <u>http://investmentproductresearch.com/assets/inc/ajax.inc.php?action=getPriips&productId=503&format</u> <u>=html</u>
- b) Via Develop page: click the "PRIIPs" analysis button for results

#### Notable results are:

PRIIPs Field	Description
RHP (y)	The "recommended holding period" or Duration post-strike
Market Risk Measure	The PRIIPs MRM
Credit Risk Measure	The PRIIPs CRM
SummaryRiskIndicator	The PRIIPs SRI

VaR97.5 (%)	The actual VaR used to calculate the VaR equivalent volatility			
One-off EntryCosts RIY (%pa)	The ratio of (IPR FairValue <sup>12</sup> ) / (offer price), annualized by the product's			
	real-world Duration			
Stresstest Scenario	Uses the RTS stresstest methodology			
Unfavourable Scenario	Uses the 10 <sup>th</sup> percentile of the real-world annualized returns distribution			
Moderate Scenario	Uses the 50 <sup>th</sup> percentile of the real-world annualized returns distribution			
Favourable Scenario	Uses the 90 <sup>th</sup> percentile of the real-world annualized returns distribution			

<sup>&</sup>lt;sup>12</sup> If IPR does not calculate a FairValue (we currently only support UKX, SX5E and SPX underlyings), we use the average of the PRIIPs simulated present values

# **Tables and Charts**

#### **PAYOFF ANALYSIS TABLE**

We calculate the probability of each event and the return that an investor would receive through a product's life under each scenario

		Future Stresstest				Historic Backtest			
		Non Credit Adj		Credit Adj		Non Credit Adj			
Description	Levels	Prob	Payoff	%pa	Payoff	%pa	Prob	Payoff	%pa
KO y2	100%E	63.9	120.0	11.4	119.1	10.8	75.8	120.0	11.4
KO y3	100%E	11.0	130.0	10.1	127.3	9.2	3.0	130.0	10.1
KO y4	100%E	5.6	140.0	9.4	134.4	8.1	2.3	140.0	9.4
KO y5	100%E	3.5	150.0	8.9	140.3	7.3	2.4	150.0	8.9
KO y6	75%E	8.2	160.0	8.5	146.7	6.8	9.0	160.0	8.5
Maturity - barrier hit	60%E	3.7	49.1	-12.6	45.0	-14.0	0.4	58.3	-9.8
Maturity	100%E	4.2	100.0	-0.5	91.5	-2.1	7.2	100.0	-0.5

For callable products we calculate the chance of early maturity at each call date. We also calculate the probability of the product reaching full term. At maturity we calculate the chance that any barrier has been breached.

Where products offer a conditional coupon or a coupon that accumulates over time, we calculate the chance that the coupon is paid, and the amount that an investor can expect

# **CHARTS**

## **All-products scatter chart**

The main Listing scatter chart features:

- An "efficient frontier" of sorts a straight line connecting 6y GBP swaps with UK equities (total return) held 6y
- Only displayed products are plotted, so you can use the various criteria in the SearchCriteria box isolate the products you want
- Customize X and Y axes on your Profile page
- Hovering over a plotted point gives tooltip information, and clicking it takes you to the Listing entry for that product (and magnifies that point for easier identification)

## **Per-product charts**

Our website provides each product with the following charts:

#### Historic Back-Test



Highcharts.com

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This is the Historic Back-test analysis (described earlier) displayed in chart form.

#### Future Stress-Test





This is the Future Stress-test analysis (described earlier) displayed in chart form.

#### Outlook



This shows Historic Back-test information:

- Index series: scaled to 1.0 on StrikeDate
- Payoffs: payoff<sup>13</sup> for a product started on each date, plotted at that start date
- WorstIndex: performance of worst index over full maturity starting on each date, plotted at that start date

# **Additional charts**

The following charts can be made available on request:





We compare the product's gains and losses with that of a benchmark asset held 6y. The right hand box represents the product's expected conditional gains and the left hand box losses. The height of each box is it's

<sup>&</sup>lt;sup>13</sup> 1.2 for example means a final value of 120%

the expected conditional (annualised) return. The width of each box represents its probability. The corresponding values for the benchmark are the wireframe boxes. The points within each box are at their expected (unconditional) returns, i.e. expected Conditional Return times probability. The smaller points are for the benchmark.

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This chart allows an investor to visualise the risk and return trade-off for this product versus a benchmark investment. In this instance it is clear that compared with an investment in a portfolio of 40% UK equity, 60% global bonds the product offers the following

- A similar chance of making a profit
- The conditional profit is somewhat higher
- A similar chance of making a loss
- But the conditional loss is much larger





We compare the product's expected gains and losses with the best in the same category (those with the most efficient gain to loss ratio).

This is a standard risk/ return efficient frontier chart. Products placed in the North East corner of this chart will have a better risk/return ratio than products at the bottom right. If one product is placed above another it offers a greater return for a similar level of risk. If it placed to the left, it offers less risk for the same level of expected returns. We automatically select 5 other products for comparison based on the product type.

Product Potential Payoffs, Triggers, Barriers





We plot the product's:

- Potential payoffs at different points in its life (blue dots)
- Barriers (green dots) levels which the underlyings must reach for the corresponding contingent payoff to be made
- Triggers (red dots) levels which, if reached, trigger potential contingent payoffs, such as a down-and-in put.

We also plot historical levels for the underlyings, normalised to 1 on the product's strike date



#### Product Potential Payoffs vs Final Asset Value – Future Stress Test

We show how product payoff depends on the final asset return, using our future stress test methodology; for example this product (which is now somewhat in-the-money):

- Has higher payoffs when the underlying gain is more modest (very high underlying returns lead to early kickout); this is particularly noticeable with the final year 75% kickout
- Pays back only capital when the final asset return is in the range minus 25% to minus 40%

- Loses capital only when the final asset return is below minus 40%, losing 40% when the final asset return is -40% and further 1-for-1 losses at lower levels

#### Distribution of Annualised Returns – Future Stress Test



From the results of our future stress test, we plot the distribution of annualised returns, using 1% return buckets; for this product:

- The significant 12% return bucket reflects kickout in year2
- Lower returns reflect kickouts in other years
- Zero return represents products which do not kickout and where the 60% trigger is not met
- The negative returns reflect products where the 60% trigger is met if the product did not kickout

# Appendix A – detailed example of volatility calculation

Probability	Payoff
80%	1.10
10%	1.00
4%	0.85
3%	0.80
2%	0.75
1%	0.70

Consider a synthetic zero product, with the following payoffs at maturity

The average annualized return is 5.8% and the traditional volatility using all the outcomes would be 10.6%. The IPR volatility however, concentrating more on potential losses, is 16.1%. Here is how distributions of return, based on these different volatilities compare:





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